

# On the Accuracy of Direct Extraction of the Heterojunction-Bipolar-Transistor Equivalent-Circuit Model Parameters $C_\pi$ , $C_{BC}$ , and $R_E$

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**Abstract**—Several basic small-signal equivalent-circuit models for bipolar transistors lead to simple analytical expressions for the model parameters in terms of measured values. This paper investigates the accuracy of these expressions for real transistors by applying the direct extraction equations to more complicated small-signal models. The extraction of the base/collector capacitance, base/emitter capacitance, and emitter resistance are considered. Analytically derived trends are illustrated using measurements on small-area high-speed InP/GaAsSb/InP double heterojunction bipolar transistors.

**Index Terms**—Circuit modeling, heterojunction bipolar transistor (HBT), parameter extraction, small signal.

## I. INTRODUCTION

IN THE high-frequency characterization of microwave transistors, small-signal models are often used to parametrize complicated behaviors with relatively simple equations. A small-signal model is preferably designed so that the model parameters represent something physical in the transistor. There are fundamental limitations in using lumped-element circuit models to describe physical structures such as a bipolar transistor, but such small-signal models can be remarkably effective at describing transistor behavior across a wide range of frequencies. As well, many model parameters may directly and unambiguously be correlated with physical quantities. This allows meaningful feedback between characterization/analysis and the design/fabrication of transistors. Indeed, there is much information one can obtain from small-signal parameters without obtaining the complete small-signal model for a transistor. The magnitude of a capacitance, for instance, tells us about device area and doping levels.

This paper examines methods used for the direct extraction of certain small-signal parameters: the base/collector capacitance,

base/emitter capacitance, and emitter resistance. These parameters can be extracted directly by manipulation of the basic small-signal model equations; a parameter can be expressed as a simple function of the  $Y$ - or  $Z$ -parameters. However, real transistors need to be described by more complicated models. By applying the simple direct extraction equations to more complicated small-signal models, the validity of these equations for real transistors can be investigated analytically. We reinforce these findings with experimental results on InP/GaAsSb/InP double heterojunction bipolar transistors (DHBTs) fabricated and characterized at Simon Fraser University, Burnaby, BC, Canada [1].

Previous papers on bipolar transistor modeling discussed the frequency ranges of validity of various equations used in direct parameter extraction, and some have examined the sensitivity of extracted parameters to model inaccuracies. Pehlke and Pavlidis only considered the effects of external inductances on extracted base/collector capacitances [2]. The work by Spiegel *et al.* looked at extracted base/collector capacitances with the base/collector divided into an intrinsic and extrinsic region [3]. Li and Prasad performed direct parameter extraction by dividing up the frequency axis into a set of ranges, determined by characteristic delay times of the transistors [4]. They did not, however, look at the base/emitter capacitance, and the present work extends on theirs in examining the validity of approximations made for the determination of the emitter resistance and base/collector capacitance. Horng *et al.* studied and exploited the effects of emitter inductances on directly extracted parameters [5]. Ouslimani *et al.* follow the work of [4] and describe more sophisticated methods for direct parameter extraction, which prescribes frequency ranges of validity for the many required model equations [6]. In this paper, various alternatives for the direct extraction of the base/collector capacitance and external emitter resistance are compared and contrasted: manipulation of the basic model equations indicates that direct extraction from both  $Y$ - and  $Z$ -parameters is possible, and (in the simplest models) both give the same results.

In Section II, two well-known basic bipolar transistor models—the  $T$ -equivalent and hybrid- $\pi$  models—are presented in a tutorial manner, and the effects of additional parameters on the model equations are examined. The direct extraction of the base/collector capacitance  $C_{BC}$ , base/emitter

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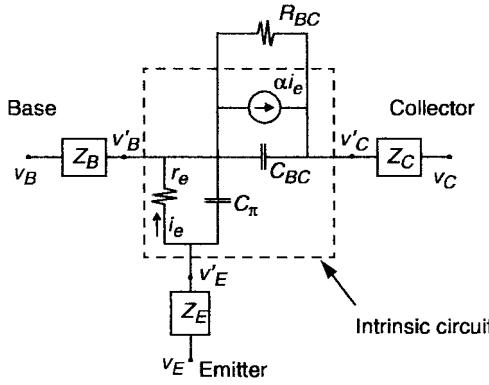


Fig. 1. Simplified  $T$  equivalent circuit for bipolar transistor. Intrinsic circuit is indicated inside the dashed box. External impedances are represented by  $Z_E$ ,  $Z_B$ , and  $Z_C$ . Finite output impedance is represented by  $R_{BC}$ . Pad capacitances are not shown.

capacitance  $C_\pi$ , and emitter resistance  $R_E + r_e$  using various techniques are then analyzed. A summary of findings concludes this paper.

## II. BASIC MODEL EQUATIONS

In this section, two well-known basic bipolar transistor equivalent-circuit models are reviewed: the  $T$ -equivalent and hybrid- $\pi$  circuit models. Circuit equations for these basic models are given, and some complications to the simple models are presented.

### A. $T$ Equivalent-Circuit Model

Fig. 1 shows the simplified  $T$  equivalent circuit for a bipolar transistor. The part inside the dashed box is the intrinsic simplified  $T$  equivalent-circuit model, and the impedances surrounding the intrinsic transistor ( $Z_E$ ,  $Z_B$ , and  $Z_C$ ) consist of a resistor and an inductor in series. The intrinsic  $Y'$ -parameters are

$$Y' = \begin{bmatrix} (1-\alpha) \frac{1}{r_e} + j\omega(C_\pi + C_{BC}) & -j\omega C_{BC} \\ \frac{\alpha}{r_e} - j\omega C_{BC} & j\omega C_{BC} \end{bmatrix}. \quad (1)$$

For a compact  $Z$ -parameter representation, the current generator term is defined in terms of the total emitter current  $i_e$  entering the resistance  $r_e$  giving

$$Z' = \begin{bmatrix} Z_{BE} & Z_{BC} \\ Z_{BC} - \alpha_F Z_{BC} & Z_{BC} + (1 - \alpha_F) Z_{BC} \end{bmatrix} \quad (2)$$

where the impedances are  $Z_{BC} = 1/(1/r_e + j\omega C_\pi)$  and  $Z_{BC} = 1/j\omega C_{BC}$ .

There is a subtle difference between the two approaches, as discussed in [8]. The transistor parameters  $\alpha_F$  and  $\alpha$  are related to the dc common base current gain  $\alpha_0$ , and include terms to account for various delay terms. The parameter  $\alpha$  includes modifications to the magnitude and phase as functions of frequency as a consequence of the base/collector depletion layer transit times giving

$$\alpha = \alpha_0 \left[ \frac{\sin(\omega\tau_C)}{\omega\tau_C} \right] \exp(-j\omega\tau) \quad (3)$$

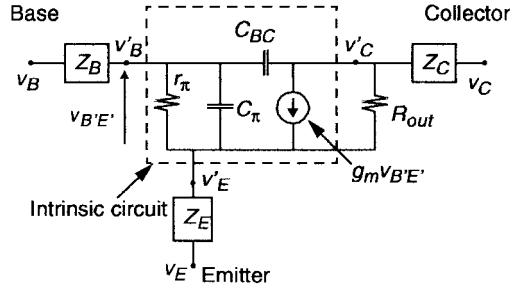


Fig. 2. Simplified hybrid- $\pi$  equivalent circuit for bipolar transistor. The intrinsic circuit is indicated inside the dashed box. External impedances (a resistor and inductor in series) are represented by  $Z_E$ ,  $Z_B$ , and  $Z_C$ . Finite output impedance is represented by  $R_{out}$ . Pad capacitances are not shown.

where  $\tau_C$  is the collector transit time and  $\tau$  is an empirical delay time consisting of the collector transit time and a small portion of the base transit time. However, the base/emitter delay is absorbed by the base/emitter  $RC$  circuit. In contrast, the parameter  $\alpha_F$ , which is used in the  $Z$ -parameter version of the  $T$  equivalent circuit, does include the base/emitter delay. It is given by [8]

$$\alpha_F = \frac{\alpha}{1 + \frac{j\omega}{\omega_B}} \quad (4)$$

where  $\omega_B$  represents an additional first-order magnitude and phase shift caused by the base/emitter delay. This latter is used in the  $Z$ -parameter version of the small-signal model.

### B. Hybrid- $\pi$ Equivalent-Circuit Model

Fig. 2 shows the simplified  $T$  equivalent circuit for a bipolar transistor. The intrinsic  $Y'$ -parameters for this two port can be shown to be

$$Y' = \begin{bmatrix} \frac{1}{r_\pi} + j\omega(C_\pi + C_{BC}) & -j\omega C_{BC} \\ g_m - j\omega C_{BC} & j\omega C_{BC} \end{bmatrix}. \quad (5)$$

Note that the hybrid- $\pi$  and  $T$  equivalent model equations are identical if the following substitutions are made:

$$r_\pi = \frac{r_e}{1 - \alpha} \text{ and } g_m = \frac{\alpha}{r_e}. \quad (6)$$

Otherwise, all parameters are equivalent, and notably the base/emitter and base/collector capacitances are unchanged. Extrinsic parameters are also unchanged.

### C. Finite Output Impedance

The output impedance is added in one of two ways. It may be added as a conductance between the base and collector, as is usually the case for  $T$  equivalent circuits (Fig. 1). In this case, the effects of the output conductance are added by replacing each instance of  $j\omega C_{BC}$  with  $j\omega C_{BC} + 1/R_{BC}$ .

Or it is added as a conductance between the emitter and collector, as is usually drawn for hybrid- $\pi$  equivalent circuits (Fig. 2). In this second case, the output conductance is added as an admittance to the intrinsic  $Y$ -parameters

$$Y' = \begin{bmatrix} Y'_{11} & Y'_{12} \\ Y'_{21} & Y'_{22} + \frac{1}{R_{out}} \end{bmatrix}. \quad (7)$$

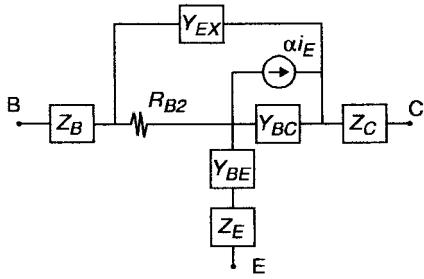


Fig. 3. Wei and Hwang's full  $T$  equivalent circuit for bipolar transistor [10]. External capacitances are not shown.

#### D. Extrinsic/Intrinsic Base/Collector Capacitance: $Y$ -Parameters

More accurate bipolar transistor models must take into account the extrinsic and intrinsic components of the base/collector capacitance, which are separated by an internal base resistance; this distributed nature of the base/collector junction is very important in estimating the  $f_{MAX}$  of a heterojunction bipolar transistor (HBT) [9]. A  $T$  equivalent circuit with this modification is shown in Fig. 3. The model equations in terms of the simplified intrinsic  $Y$ -parameters (not including external impedances) are

$$\begin{aligned} Y_{11} &= \frac{Y'_{11}}{R_{B2}Y'_{11} + 1} + j\omega C_{EX} \\ Y_{12} &= \frac{Y'_{12}}{R_{B2}Y'_{11} + 1} + j\omega C_{EX}. \end{aligned} \quad (8)$$

Resistances in parallel with  $C_{EX}$  are not included in the above expressions.

#### E. Extrinsic/Intrinsic Base/Collector Capacitance: $Z$ -Parameter Expressions

For some calculations it is more convenient to use  $Z$ -parameter expressions for the  $T$  equivalent-circuit model including the effects of the distributed base/collector junction. Wei and Hwang [10] used the equivalent-circuit model of Fig. 3, which conveniently includes the parasitic series inductances  $Z_B$ ,  $Z_E$ , and  $Z_C$ . Note that to allow for a resistance in parallel with  $C_{BC}$  and  $C_{EX}$ , these terms are written as generic admittances  $Y_{BC}$  and  $Y_{EX}$ . Wei and Hwang provide the following model equations:

$$\begin{aligned} Z_{11} &= \frac{[(1 - \alpha_F)Z_{BC} + Z_{EX}]R_{B2}}{Z_{BC} + Z_{EX} + R_{B2}} + Z_{BE} + Z_B + R_E \\ Z_{12} &= \frac{(1 - \alpha_F)Z_{BC}R_{B2}}{Z_{BC} + Z_{EX} + R_{B2}} + Z_{BE} + Z_E \\ Z_{21} &= \frac{[-\alpha_F Z_{EX} + (1 - \alpha_F)R_{B2}]Z_{BC}}{Z_{BC} + Z_{EX} + R_{B2}} + Z_{BE} + Z_E \\ Z_{22} &= \frac{(1 - \alpha_F)Z_{BC} + (Z_{EX} + R_{B2})}{Z_{BC} + Z_{EX} + R_{B2}} + Z_{BE} + Z_C + Z_E. \end{aligned} \quad (9)$$

(Note that the current generator refers to the terminal emitter current, hence, the use of  $\alpha_F$  instead of  $\alpha$ .)

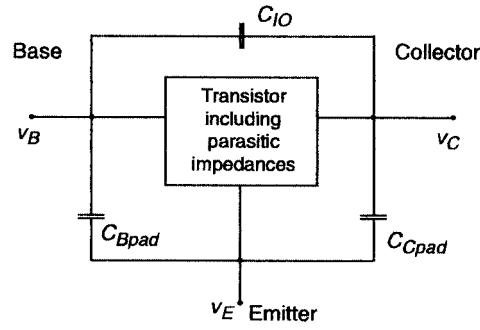


Fig. 4. Schematic showing placement of external parasitic capacitances:  $C_{B\text{pad}}$  is the base pad capacitance,  $C_{C\text{pad}}$  is the collector pad capacitance, and  $C_{IO}$  is the input/output capacitance.

#### F. Adding External Capacitances and Impedances

To add external impedances to any of the above circuits, the impedances (shown in Fig. 1) are added to the  $Z$ -parameters in series as follows:

$$Z = \begin{bmatrix} Z'_{11} + Z_B + Z_E & Z'_{12} + Z_E \\ Z'_{21} + Z_E & Z'_{22} + Z_C + Z_E \end{bmatrix} \quad (10)$$

where  $Z_i = R_i + j\omega L_i$  for each of the emitter, base, and collector terminals. When deembedding of parasitics is performed, the pad inductances should be removed almost entirely, but some external series resistances will remain because ohmic contacts are generally considered to be part of the complete transistor.

The pad capacitances, shown in the small-signal equivalent-circuit model in Fig. 4, are added using  $Y$ -parameters [11]. The  $Z$ -parameters of the intrinsic device with external impedances are converted to  $Y$ -parameters, and then the following calculation is made:

$$Y = Y' + Y_{\text{pad}} = \begin{bmatrix} Y'_{11} + Y_{B\text{pad}} + Y_{IO} & Y'_{12} - Y_{IO} \\ Y'_{21} - Y_{IO} & Y'_{22} + Y_{C\text{pad}} + Y_{IO} \end{bmatrix} \quad (11)$$

where  $Y_i = j\omega C_i$  for each of the capacitive admittances.

In this study, the external pad impedances, inductances, and capacitances have been removed by the inverse procedure, with capacitances and impedances having been determined from dummy OPEN and SHORT pads. However, some residual parasitics from imperfect deembedding always remain. Generally, inductances for larger devices and capacitances for smaller devices are the important parasitic elements at high frequencies.

### III. BASE/COLLECTOR CAPACITANCE EXTRACTION

#### A. From Basic Model Equations

A base/collector capacitance may be extracted using the  $T$  equivalent-circuit  $Z$ -parameter relations in (2) as follows:

$$\tilde{C}_{BC}(Z) \equiv \frac{1}{\omega \text{Im}\{Z_{22} - Z_{21}\}}. \quad (12)$$

(This is identically equivalent to the  $H$ -parameter expression for base-collector capacitance used in [2].) As will be shown later, a better approach is to take the imaginary part of the admittance instead [12] as follows:

$$C_{BC}(Z) \equiv \text{Im} \left\{ \frac{1}{\omega \{Z_{22} - Z_{21}\}} \right\}. \quad (13)$$

Based on the simplified equivalent-circuit models, the same value for base/collector capacitance  $C_{BC}(Y)$  appears to be extracted using  $Y$ -parameters using the relation in (1) as follows:

$$C_{BC}(Y) \equiv \frac{\text{Im}\{Y_{12}\}}{\omega}. \quad (14)$$

However, inaccuracy can result from the use of  $C_{BC}(Y)$  when the effect of extrinsic/intrinsic base/collector capacitance is included. By putting (1) into (8), we obtain for  $Y_{12}$

$$Y_{12} = \frac{-j\omega C_{BC}}{R_{B2} \left( (1-\alpha) \frac{1}{r_e} + j\omega (C_\pi + C_{BC}) \right) + 1} - j\omega C_{EX}. \quad (15)$$

The base/emitter capacitance and base/collector capacitance in the denominator are ignored (since  $\omega R_{B2}(C_\pi + C_{BC}) \ll 1$  at our measurement frequencies), thus,

$$C_{BC}(Y) \approx \frac{C_{BC}}{(1-\alpha) \frac{R_{B2}}{r_e} + 1} + C_{EX}. \quad (16)$$

For larger devices,  $r_e$  is small (order of  $1 \Omega$ ), and  $R_{B2}$  can be substantial (tens of ohms). For a typical  $\beta$  (approximately 50) giving  $(1-\alpha) \sim 0.02$ , the denominator in the first term may not be that close to unity. This technique, therefore, fails under not too uncommon circumstances.

When a transistor is in forward active operation (typical for high-frequency characterization), the  $Y$ -parameter technique may, therefore, lead to inaccuracies. Potentially, in a transistor with sufficiently low dc gain and large ratios between the base and emitter resistances, the different values obtained  $C_{BC}(Y)$  and  $C_{BC}(Z)$  may be used to help separate the intrinsic and extrinsic base/collector capacitance components.

On the other hand, when a transistor is “cold”—very weakly forward active biased (at or below the base/emitter turn-on voltage) or in cutoff (both base/collector and base/emitter junctions reverse biased)—then the current gain  $\alpha$  may be very small, hence,  $(1-\alpha) \sim 1$ , but  $r_e$  will be very large. Thus, the denominator in (16) will go to unity as follows:

$$C_{BC}(Y) \approx C_{BC} + C_{EX}. \quad (17)$$

Thus,  $C_{BC}(Y)$  is accurate even for larger emitter transistors when they are under “cold” bias or in cutoff.

The base/collector capacitance  $C_{BC}(Z)$  extracted from  $Z$ -parameters, in contrast, is well behaved in transistors under forward active operation [3]. From Wei and Hwang’s expression for the model  $Z$ -parameters in (9) (neglecting external impedances)

$$\begin{aligned} \frac{1}{Z_{22} - Z_{21}} &\approx \frac{Z_{BC} + Z_{EX} + R_{B2}}{Z_{BC} Z_{EX}} \\ &= Y_{BC} + Y_{EX} + \frac{R_{B2}}{\frac{1}{Y_{BC}} \frac{1}{Y_{EX}}} \\ \therefore C_{BC}(Z) &\equiv \text{Im} \left\{ \frac{1}{\omega \{Z_{22} - Z_{21}\}} \right\} = C_{BC} + C_{EX}. \quad (18) \end{aligned}$$

Therefore, the extracted base/collector capacitance equals the sum of the intrinsic and extrinsic capacitances. Comparisons of the  $Y$ -parameter-extraction technique to the  $Z$ -parameter technique are shown in Fig. 5 for a narrow emitter stripe and Fig. 6

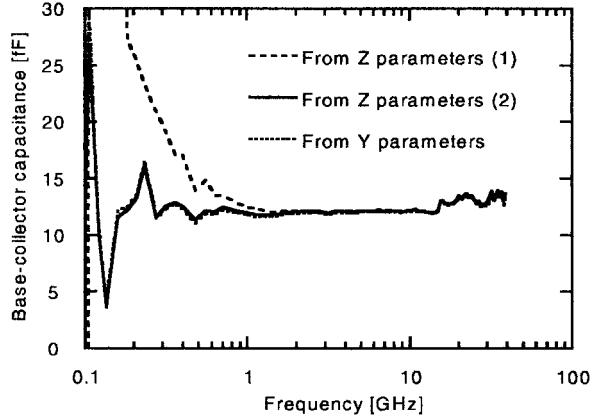


Fig. 5. Comparison of extracted base/collector capacitance of  $0.5 \times 12 \mu\text{m}^2$  emitter metal device using three different extraction techniques: (dashed line) from  $Z$ -parameters using (12); (solid line) from  $Z$ -parameters using (13); (dotted line) from  $Y$ -parameters using (14). The values for the two latter techniques are nearly identical for this device. The increased apparent capacitance when using (12) results from the finite output impedance.

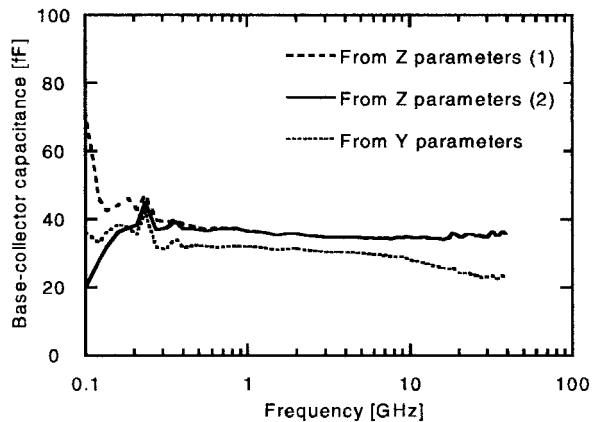


Fig. 6. Comparison of extracted base/collector capacitance of  $2.0 \times 24 \mu\text{m}^2$  emitter metal device using three different extraction techniques: (dashed line) from  $Z$ -parameters using (12); (solid line) from  $Z$ -parameters using (13); (dotted line) and from  $Y$ -parameters using (14). The reduced value of base capacitance obtained from  $Y$ -parameters is because of the large  $R_{B2}$  related to spreading resistance under the emitter. Also, the bias current is large so  $r_e$  is small. Compare with Fig. 5, which is for a device fabricated simultaneously, but with a narrower emitter.

for a wider emitter stripe. When the base spreading resistance is large and the emitter resistance is small, then the  $R_{B2}$  term causes  $C_{BC}(Y)$  to drop from the limiting value of  $C_{BC} + C_{EX}$ .

#### B. Effects of Pad Capacitances

The input pad capacitance  $C_{B\text{pad}}$  does not affect  $C_{BC}(Z)$  because  $C_{BC}(Z)$  is derived from the output  $Z$ -parameters  $Z_{22}$  and  $Z_{21}$ . An input/output capacitance will add to  $C_{BC}(Z)$  in the same way that the intrinsic/extrinsic parts of the base/collector capacitance add. The effect of the output pad capacitance is more interesting. For the circuit shown in Fig. 4, with  $C_{B\text{pad}} = 0$  and  $C_{IO} = 0$ , the extrinsic  $Z_{21}$  and  $Z_{22}$  in terms of intrinsic  $Z$ -parameters  $Z'$  become

$$\begin{aligned} Z_{21} &= Z'_{21} \left( 1 - \frac{Z'_{22}}{Z'_{22} + Z_p} \right) \\ Z_{22} &= \frac{Z_p Z'_{22}}{Z'_{22} + Z_p} \end{aligned} \quad (19)$$

where we define  $Z_p = 1/j\omega C_{C\text{pad}}$ . The  $Z$ -parameters of the intrinsic circuit are assumed to be

$$Z' = \begin{bmatrix} Z_{\text{BE}} & Z_{\text{BE}} \\ Z_{\text{BE}} - \alpha_F Z_{\text{BC}} & Z_{\text{BE}} - (1 - \alpha) Z_{\text{BC}} \end{bmatrix} \quad (20)$$

for simplicity.  $C_{\text{BC}}$  is calculated using (19) and (20) as follows:

$$\frac{1}{Z_{22} + Z_{21}} = \frac{Z_{\text{BE}} - (1 - \alpha_F) Z_{\text{BC}} + Z_p}{Z_p Z_{\text{BC}}}. \quad (21)$$

In transistors under forward active bias,  $Z_{\text{BE}}$  may be ignored because it is much smaller than the other two impedances. After substituting for the definitions of  $Z_{\text{BC}}$  and  $Z_p$ , and using (13) to find  $C_{\text{BC}}(Z)$ , this becomes

$$\begin{aligned} \frac{1}{Z_{22} - Z_{21}} &\approx (1 - \alpha_F) j\omega C_{C\text{pad}} + j\omega C_{\text{BC}} \\ \therefore C_{\text{BC}}(Z) &\equiv \text{Im} \left\{ \frac{1}{\omega \{Z_{22} - Z_{21}\}} \right\} \approx (1 - \alpha_0) C_{C\text{pad}} + C_{\text{BC}}. \end{aligned} \quad (22)$$

Therefore, the extracted base/collector capacitance  $C_{\text{BC}}(Z)$  will include a contribution from the collector pad capacitance. As long as the current gain is high, then this contribution should not be important, except on very small devices. For 2000-Å collectors, the base/collector capacitance is approximately  $0.5 \text{ fF}/\mu\text{m}^2$ , whereas the error in pad deembedding should not exceed more than a few femtofarads. To put in some numbers in a realistic “worst-case” example, let us assume a deembedding error of 2 fF, a gain of ten, and a base-collector area of  $2 \mu\text{m}^2$  (i.e.,  $C_{\text{BC}} \sim 1 \text{ fF}$ ). The deembedding error will then be 0.2 fF or 20%.

The assumption made in (22) (that  $Z_{\text{BE}}$  is small) no longer holds for devices under “cold” bias. Under such conditions, the dynamic emitter resistance  $r_e$  is very large and the extracted base/collector capacitance will instead be

$$\begin{aligned} \frac{1}{Z_{22} - Z_{21}} &= \frac{\frac{1}{Y_{\text{BE}}} + \frac{(1 - \alpha_F)}{Y_{\text{BC}}} + \frac{1}{Y_p}}{\frac{1}{Y_p Y_{\text{BC}}}} \\ &= \frac{Y_p Y_{\text{BC}}}{Y_{\text{BE}}} + (1 - \alpha_F) Y_p + Y_{\text{BC}} \\ &= \left( \frac{C_{\text{BC}}}{C_\pi} \right) j\omega C_{C\text{pad}} + (1 - \alpha_F) j\omega C_{C\text{pad}} \\ &\quad + j\omega C_{\text{BC}} \\ \therefore C_{\text{BC}}(Z) &\equiv \text{Im} \left\{ \frac{1}{\omega \{Z_{22} - Z_{21}\}} \right\} \\ &\approx \left( \frac{C_{\text{BC}}}{C_\pi} \right) C_{C\text{pad}} + (1 - \alpha_F) C_{C\text{pad}} + C_{\text{BC}}. \end{aligned} \quad (23)$$

Thus, the contribution from the collector pad capacitance will be multiplied by the ratio of the base/collector and base/emitter capacitances. In our devices, the ratio between these junction capacitances typically ranges from about unity for 2-μm emitter devices to as high as ten for submicrometer emitter devices ( $C_\pi$  is small in “cold” bias). Since the collector pad capacitance is on

the order of tens of femtofarads, an error of a few femtofarads is to be expected from deembedding. Small-emitter devices under “cold” bias may, therefore, have very large percentage errors in  $C_{\text{BC}}(Z)$  associated with inaccurate deembedding of  $C_{C\text{pad}}$ .

The extracted base/collector capacitance  $C_{\text{BC}}(Y)$  is sensitive only to the base/collector pad capacitance  $C_{IO}$  since it is obtained from  $Y_{12}$  [see (11)].

### C. Effects of Finite Output Impedance

There are several effects on the extracted base/collector capacitance  $C_{\text{BC}}(Z)$  when there is finite output impedance. First, the effect of an output conductance in parallel with the base/collector capacitance (Fig. 1) is considered. If  $C_{\text{BC}}$  is extracted using the formula for  $C_{\text{BC}}(Z)$  in (12) then, at low frequencies,  $C_{\text{BC}}$  will include a contribution from the finite real output conductance because it is acting in parallel to the base/collector capacitance  $j\omega C_{\text{BC}} \Rightarrow j\omega C_{\text{BC}} + G_{\text{BC}}$ . The characteristic frequency below which this effect appears is  $1/2\pi f \approx R_{\text{BC}} C_{\text{BC}}$ , which is typically below 1 GHz. If, however, the formula of (13) is used, i.e., the capacitance is assumed to be parallel to a conductance and, thus, it forms the imaginary part of an admittance, then this effect disappears entirely. Fig. 5 shows the improved behavior at low frequencies when using (13) instead of (12).

However, an output conductance parallel with the intrinsic base/collector capacitance may act to increase the extracted capacitance [12], [13]

$$\begin{aligned} C_{\text{BC}}(Z) &\equiv \text{Im} \left\{ \frac{1}{\omega \{Z_{22} - Z_{21}\}} \right\} \\ &= C_{\text{BC}} + C_{\text{EX}} (1 + R_{B2} G_{\text{BC}}). \end{aligned} \quad (24)$$

For our DHBTs, the  $R_{B2} G_{\text{BC}}$  is much smaller than unity and this effect can be ignored.

The finite output impedance interacting with the collector pad capacitance may cause a similar problem. By taking (22) and replacing the collector pad admittance with the output admittance  $1/R_{\text{out}}$  (compare Figs. 2 and 4), the extracted  $C_{\text{BC}}(Z)$  becomes

$$\begin{aligned} \frac{1}{Z_{22} - Z_{21}} &= \frac{1 - \alpha_F}{R_{\text{out}}} + j\omega C_{\text{BC}} \\ &\approx \frac{1 - \alpha_0 (1 - j\omega \tau_d)}{R_{\text{out}}} + j\omega C_{\text{BC}} \\ \therefore C_{\text{BC}}(Z) &= \frac{\alpha_0 \tau_d}{R_{\text{out}}} + C_{\text{BC}} + \text{imaginary term}. \end{aligned} \quad (25)$$

For simplicity, the first-order behavior of  $\alpha_F$  is modeled using a single time constant  $\tau_d$ . The extracted base/collector capacitance is increased because of the additional first term. Fortunately,  $R_{\text{out}}$  is very large (kiloohms) and  $\tau_d$  is very small (< picosecond) and, thus, the additional term is negligible in our devices.

### D. Effects of Parasitic Impedances on $C_{\text{BC}}(Z)$

From the  $Z$ -parameters expressions (9) and the definition for  $C_{\text{BC}}(Z)$  in (12), only the collector impedance should affect the extracted  $C_{\text{BC}}$  as follows:

$$C_{\text{BC}}(Z) = \frac{C_{\text{BC}}}{1 - \omega^2 L_C C_{\text{BC}}}. \quad (26)$$

At higher frequencies, the extracted base/collector capacitance, therefore, increases. If the expression (13) for  $C_{BC}(Z)$  is used instead, then

$$C_{BC}(Z) = C_{BC} \times \frac{(1 - \omega^2 L_C C_{BC})}{(1 - \omega^2 L_C C_{BC})^2 + (\omega R_C C_{BC})^2}. \quad (27)$$

The terms  $\omega^2 L_C C_{BC}$  and  $(\omega R_C C_{BC})^2$  are both small for typical high-speed devices, thus, the external impedances should not affect the apparent  $C_{BC}(Z)$ .

#### IV. BASE/EMITTER CAPACITANCE EXTRACTION

##### A. Introduction

While there have been published attempts to obtain the base/emitter capacitance  $C_\pi$  by complicated manipulations (Li and Prasad [4] and Wei and Hwang [10]), others such as Spiegel *et al.* [3] and Pehlke and Pavlidis [2] state that this capacitance cannot be directly extracted from measured  $S$ -parameters. On the other hand, Chang *et al.* state that the base/emitter capacitance is directly determined from the input admittance when the base/collector and input pad capacitances are known [14]. These discrepancies may arise because the  $\alpha$  term and the capacitance  $C_\pi$  cannot be obtained independently. To complicate matters, the capacitance  $C_\pi$  necessarily consists of a depletion capacitance depending on the base/emitter voltage, and a diffusion capacitance proportional to the collector current.

That is not to say that it is impossible to estimate the base/emitter capacitance from  $S$ -parameters. The base/emitter capacitance  $C_\pi(Y)$  appears in the basic equations in (1) and, thus,

$$C_\pi(Y) \equiv \frac{1}{\omega} \text{Im} \{Y_{11} + Y_{12}\} = \frac{1}{\omega} \text{Im} \left\{ \frac{1}{r_\pi} + j\omega C_\pi \right\}. \quad (28)$$

This appears to give the final answer. Unfortunately,  $r_\pi$  is complex. It is defined by  $r_\pi = r_e/(1 - \alpha)$ . Since  $\alpha$  is complex, the imaginary part of  $Y_{11} + Y_{12}$  must include a contribution from  $r_\pi$ . Rewriting the above (assuming small  $\omega\tau$ , hence, taking first-order approximations throughout)

$$\begin{aligned} C_\pi(Y) &= \frac{1}{\omega} \text{Im} \left\{ \frac{1 - \alpha}{r_e} + j\omega C_\pi \right\} \\ &\approx \frac{1}{\omega} \text{Im} \left\{ \frac{1 - \alpha_0(1 - j\omega\tau)}{r_e} + j\omega C_\pi \right\} \\ &= \frac{\alpha_0\tau}{r_e} + C_\pi \approx \frac{\alpha_0\tau I_C}{n_C kT} + C_\pi. \end{aligned} \quad (29)$$

A typical delay time  $\tau$  at normal biases will consist of the collector transit time and a small fraction of the base transit time, for a total of around 0.1 or 0.2 ps in the present devices (judging from minimum delay time measurements [1]). For a typical  $1 \times 12 \mu\text{m}^2$  emitter area DHBT, at a bias of 24 mA, and, thus,  $r_e \sim 1 \Omega$ . The first term, therefore, will be on the order of  $\sim 100 \text{ fF}$ , which is comparable to the typical  $C_\pi$  of 150 fF measured on a DHBT.

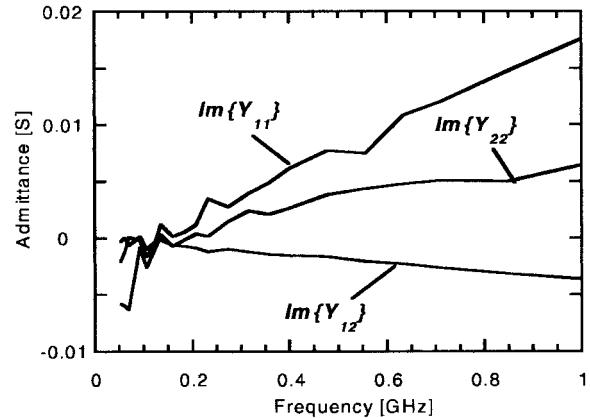


Fig. 7. Imaginary part of measured admittances  $Y_{11}$ ,  $Y_{12}$ , and  $Y_{22}$  of device described in Fig. 8. The admittances appear to have a zero intercept around 150 MHz. This is probably an artifact of imperfect calibration.

##### B. Distributed Base/Collector Effects

The above derivation used a simplified small-signal model. More accurate representations of the base/emitter capacitance  $C_\pi(Y)$  are obtained by beginning with (8), i.e., with the distributed base/collector taken into account, and putting in the intrinsic  $Y$ -parameters from (1)

$$Y_{11} + Y_{12} = \frac{\frac{1}{r_\pi} + j\omega C_\pi}{R_{B2} \left( \frac{1}{r_\pi} + j\omega (C_\pi + C_{BC}) \right) + 1}. \quad (30)$$

This is expressed in terms of the previous result (28)

$$\begin{aligned} C_\pi(Y) &= \frac{1}{\omega} \text{Im} \left\{ \left( \frac{1}{r_\pi} + j\omega C_\pi \right) \right. \\ &\quad \left. \cdot \left( 1 - \frac{\left( R_{B2} \left( \frac{1}{r_\pi} + j\omega (C_\pi + C_{BC}) \right) \right)}{1 + R_{B2} \left( \frac{1}{r_\pi} + j\omega (C_\pi + C_{BC}) \right)} \right) \right\}. \end{aligned} \quad (31)$$

What is the significance of the correction term? When  $R_{B2}$  is small, then the correction term goes to unity (the trivial case). As  $R_{B2}$  increases, both the frequency-dependent and frequency-independent parts of the correction term will tend to reduce the apparent  $C_\pi(Y)$ . The correction term may be substantial. For example, for a relatively large device, at 30 GHz, with  $R_{B2} \sim 10 \Omega$  and  $C_\pi \sim 500 \text{ fF}$ ,  $\omega R_{B2} C_\pi \sim 1$ . At low frequencies, the expression reduces to

$$C_\pi(Y) = \frac{1}{\omega} \text{Im} \left\{ \left( \frac{1}{r_\pi} + j\omega C_\pi \right) \left( 1 - \frac{(R_{B2}(1 - \alpha))}{r_e + R_{B2}(1 - \alpha)} \right) \right\}. \quad (32)$$

For typical high-speed devices, with  $\alpha \sim 0.98$ ,  $r_e \sim 1 \Omega$ , and  $R_{B2} \sim 5 \Omega$ , the apparent  $C_\pi(Y)$  will be reduced by the correction term by approximately 10%. Fig. 7 shows that, for wide

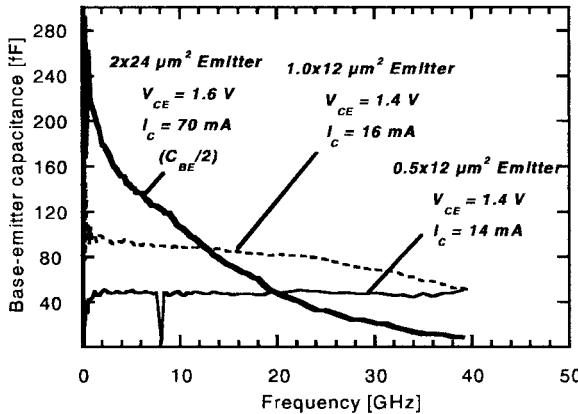


Fig. 8. Comparison of extracted base/emitter capacitance at similar current densities with identical base contact resistances, but different emitter finger widths (dimensions are nominal). Large emitter widths (i.e., large base spreading resistance devices) have poorly behaved extracted base/emitter capacitances. For the 2- $\mu\text{m}$  emitter device, the capacitance divided by two is plotted.

emitter fingers, the extracted capacitance is a strong function of frequency, while for narrow emitters, it remains essentially constant across the measured frequency range. This is because devices with wide emitter fingers will have larger internal base resistances  $R_{B2}$  than ones with narrow emitters.

### C. Output Conductance and Pad Capacitance Effects

What happens with even more complicated models? An output conductance parallel to the base/collector capacitance (i.e., each instance of  $j\omega C_{BC}$  is replaced by  $j\omega C_{BC} + 1/R_{BC}$ ) will not affect the extracted  $C_\pi(Y)$  when using the simplest model and, in the more complicated model of (31), the resistance  $R_{BC}$  is so much larger than  $r_\pi$  that it can be ignored. A conductance across the collector/emitter terminals will have no effect since it only modifies  $Y_{22}$ . If the external pad capacitances are not removed, then  $C_\pi(Y)$  will include the base pad capacitance; thus, pad deembedding is a source of error in extraction of  $C_\pi(Y)$ .

### D. Other Effects

At very low frequencies (< 1 GHz), the extracted base/emitter capacitance has been observed to decrease dramatically (see the curve for the 0.5- $\mu\text{m}$  emitter device in Fig. 7). This effect is not accounted for in the above discussion. A likely cause is the inaccuracies in the test set and/or calibration. The plots of  $\text{Im}\{Y_{11}\}$ ,  $\text{Im}\{Y_{12}\}$ , and  $\text{Im}\{Y_{21}\}$  in Fig. 8 show that they are straight lines with frequency axis intercepts at frequencies of approximately 150 MHz. This behavior cannot be described by a simple lumped-element equivalent-circuit model. Our test set (HP8516A) measures from 45 MHz to 40 GHz, and it is not unreasonable to assume that, at edges of the measurement range, the measurements may be less accurate. Therefore, other extracted parameters may also be inaccurate at very low frequencies (< 1 GHz).

## V. Emitter Resistance Extraction

The emitter resistance is an important parameter of the HBT because it can be responsible for a significant portion of the total emitter/collector delay time

$$\frac{1}{2\pi f_T} = r_e (C_{jBE} + C_{BC}) + (R_E + R_C) C_{BC} + \tau_B + \tau_C. \quad (33)$$

Here, the dynamic emitter resistance is given by  $r_e = nkT/qI_C$ , and  $R_E$  is the external series resistance (mostly the contact resistance) of the emitter. At peak cutoff frequencies for highly scaled HBTs, the dynamic resistance  $r_e$  can easily be responsible for a third of the delay time through emitter and collector charging times, while  $R_E$  is much larger than  $R_C$  and is responsible for most of the  $C_{BC}$  charging time.

### A. From Z-Parameters

The emitter resistance  $r_e + R_E$  can be found by taking the real part of  $Z_{12}$ . The first-order approximation for  $\alpha_F$  is

$$\alpha_F = \frac{\alpha_0 \left[ \frac{\sin(\omega\tau_C)}{\omega\tau_C} \right] \exp(-j\omega\tau)}{1 + j\frac{\omega}{\omega_B}} \approx \alpha_0 (1 - j\omega\tau') \quad (34)$$

where  $\tau'$  is an effective first-order time constant and, thus, the real part of  $Z_{12}$  gives

$$\begin{aligned} \text{Re}\{Z_{12}\} &= \text{Re} \left\{ \frac{(1 - \alpha_F) Z_{BC} R_{B2}}{Z_{BC} + Z_{EX} + R_{B2}} + Z_{BE} + Z_E \right\} \\ &\approx \Delta + \frac{r_e}{1 + (\omega r_e C_\pi)^2} + R_E \end{aligned} \quad (35)$$

where

$$\Delta = \text{Re} \left\{ \frac{(1 - \alpha_0 (1 - j\omega\tau')) \frac{R_{B2}}{\frac{1}{R_{BC}} + j\omega C_{BC}}}{\frac{1}{R_{BC}} + j\omega C_{BC} + \frac{1}{j\omega C_{EX}} + R_{B2}} \right\}.$$

The two right-hand terms will reduce to  $r_e + R_E$  at normal measurement frequencies because the time  $r_e C_\pi$  constant will normally be on the order of tens to a few hundreds of femtoseconds. At very low frequencies, when the  $j\omega R_{BC}(C_{EX} + C_{BC})$  term is small compared to unity, the correction term  $\Delta$  becomes

$$\Delta \approx \text{Re} \left\{ \frac{(1 - \alpha_0 (1 - j\omega\tau')) j\omega C_{EX} R_{B2} R_{BC}}{1 + j\omega R_{BC} (C_{EX} + C_{BC})} \right\} \quad (36)$$

which reduces to zero to first order. At moderate frequencies, when the  $j\omega R_{BC}(C_{EX} + C_{BC})$  term is large compared to unity, the term becomes

$$\Delta \approx \frac{(1 - \alpha_0) C_{EX} R_{B2}}{C_{EX} + C_{BC}}. \quad (37)$$

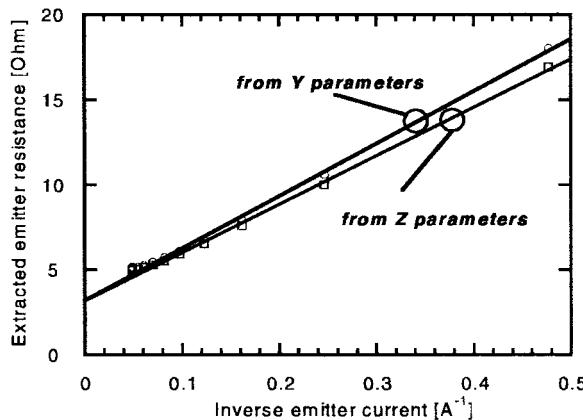


Fig. 9. Emitter resistances obtained either from the  $Z$ -parameter method (squares) or the  $Y$ -parameter method (circles). Lines are least-square fit lines to data from 2 to 16 mA. Both sets of data indicate an intercept of  $3.2 \Omega$ . This device has a  $1\text{-}\mu\text{m}$  emitter width.

For a typical gain of  $\beta = 50$ , the term  $(1 - \alpha_0)$  is around 0.02.  $C_{\text{EX}}$  is usually comparable in size or larger than  $C_{\text{BC}}$  and, thus, the capacitance ratio term will be between 0.5–1. For small devices,  $R_{B2}$  will typically be similar to the emitter resistance and, thus, the error on  $r_e + R_E$  will be a few percent. The error is added to  $r_e + R_E \Rightarrow r_e + R_E + \Delta R_{B2}$ , which is then typically plotted versus the inverse emitter current in order to determine  $R_E$  (Fig. 9). That intercept is obtained by extrapolation to infinite emitter currents, and will also be shifted by the value of the correction term.

#### B. Effects of External Parasitics on $Z$ -Parameter Method

The small-signal model used for the above derivations already includes the distributed base/collector effects, the output conductance effects, and the emitter contact resistance effect. The emitter inductance does not affect the real part of  $Z_{12}$ , and the base and collector external impedances are not part of  $Z_{12}$ . External pad capacitance effects should be small because the real part of  $Z_{12}$  should not be affected by a small external capacitance (i.e., the  $(r_e + R_E)C_{\text{pad}}$  time constant is small). However, the dummy SHORT deembedding procedure is important. If the series resistances from the SHORT are deembedded in addition to series inductances, then the pad resistance will be directly removed from the extracted emitter resistance. Thus, inaccuracies in the SHORT add directly to the extracted emitter resistance.

#### C. From $Y$ -Parameters

Another technique for the extraction of the emitter resistance is based on  $Y$ -parameters. When an impedance  $Z_E$  is added in series to the intrinsic hybrid- $\pi$  model, shown in Fig. 2, then  $1/Y_{21}$  becomes

$$\frac{1}{Y_{21}} = \frac{1 + Z_E g_m \left( 1 - \frac{Z_E Y_{\text{BE}}}{1 + Z_E Y_{\text{BE}}} \right)}{g_m \left( 1 - \frac{Z_E (Y_{\text{BE}} + Y_{\text{BC}})}{1 + Z_E Y_{\text{BE}}} \right) - Y_{\text{BC}}} \quad (38)$$

where  $Y_{\text{BE}} = 1/r_{\pi} + j\omega C_{\pi}$  and  $Y_{\text{BC}} = j\omega C_{\text{BC}}$  (neglecting the finite output impedance). At low frequencies, this reduces to

$$\frac{1}{Y_{21}} \approx \frac{1 + \frac{R_E}{r_{\pi}}}{g_m} + R_E = \frac{r_e + R_E}{\alpha}. \quad (39)$$

Since the hybrid- $\pi$  model is identically equivalent to the  $T$  equivalent model, the above can be expressed in terms of the  $T$  equivalent parameters by using the relations in (6) as follows:

$$\frac{1}{Y_{21}} \approx \frac{r_e + R_E}{\alpha}. \quad (40)$$

Thus, when this quantity is plotted against the inverse emitter current (since  $r_e = nkT/I_e$ ), the intercept with infinite emitter current will give the external emitter resistance times  $\alpha_0$ . Above dc, it may seem that the frequency dependences of  $\alpha \sim \alpha_0(1 - j\omega\tau)$  and  $j\omega C_{\pi}$  need be taken into account. However, the *magnitude* of  $(1/Y_{21})$  will not change to first order since all the time constants in the above expression are typically much smaller than the measurement frequencies.

#### D. Effects of External Parasitics on the $Y$ -Parameter Method

Of the external capacitances, only the input/output pad capacitance will affect the extracted resistance, but this capacitance is small compared with our device capacitances and can be neglected.

The emitter inductance will increase the apparent emitter resistance at high frequencies because of the decreased admittance  $Y_{21}$ . The effect of external impedances at the base and collector is somewhat more complicated. However, if the base/collector capacitance and output conductance are neglected, then it is readily shown that the collector impedance will not affect  $Y_{21}$ . The base impedance, on the other hand, will make  $1/Y_{21}$  at low frequencies go to

$$\frac{1}{Y_{21}} \approx \frac{r_e + R_E}{\alpha} + R_B \left( \frac{1 - \alpha_0}{\alpha_0} \right). \quad (41)$$

Thus, the value of the intercept of  $1/Y_{21}$  (i.e., the apparent external emitter resistance  $R_E$ ) will increase with the external base resistance. In Fig. 9, emitter resistances extracted using both the  $Y$ - and  $Z$ -parameter methods are compared for  $1\text{-}\mu\text{m}$  emitter width DHBTs. The absolute values of the apparent  $r_e + R_E$  are clearly higher for the  $Y$ -parameter method data, and the intercepts (where  $r_e$  approaches zero) are  $3.18$  and  $3.15 \Omega$  for the  $Y$ - and  $Z$ -parameter methods, respectively. The small difference appears consistent with a current gain of 80 (note that both  $Z$ -parameter methods include contributions from the base resistance). If accurate values of emitter resistance are required, then (41) can be used to calculate first-order correction terms. Additionally, the approximate external base resistance may be deembedded from measured  $S$ -parameters prior to emitter resistance calculation.

### E. Current Gain Effects: $Y$ - and $Z$ -Parameter Methods

Since the current gain is not constant across the wide range of biases, another inaccuracy stems from the dependence of the extracted resistance on  $\alpha$ . For our devices, the common emitter current gain may easily vary by a factor of four across the bias range used. Therefore,  $\alpha_0$  can easily vary by several percent. The term  $1 - \alpha_0$  will vary by approximately the same factor as the current gain. Hence, in plots such as Fig. 9, the extracted emitter resistance does not form a straight line because of the lower gain at low currents. In order to compensate for such effects, multistep parameter-extraction procedures are required, first to determine the base resistance of a device, then to determine the current gain at each bias, and finally to calculate the total emitter resistance by either the  $Y$ - or  $Z$ -parameter methods.

### VI. SUMMARY

Base/collector capacitance extraction for forward active biased HBTs using the  $Z$ -parameter method reliably gives the total intrinsic and extrinsic capacitance. Parasitic input/output capacitances directly add to the extracted base/collector capacitance, and parasitic output capacitances add a small term that is proportional to the common-base current gain. Finite output impedance is important only at low frequencies. Parasitic inductances at the collector increase the extracted capacitance. Base/collector capacitance extraction for “cold” HBTs should be performed using the  $Y$ -parameter method.

For base/emitter capacitance extraction, there is some difficulty in obtaining meaningful values of this capacitance because its first-order behavior can be accounted for by the transit time term  $\tau$  in  $\alpha$ . The extracted base/emitter capacitance includes a contribution from the transit time  $\tau$ . Distributed base/collector effects do matter, more so for larger devices; very small devices can have base/emitter capacitances extracted more reliably across a wide range of frequencies. Finite output impedance does not affect the extracted base/emitter capacitance. Of the pad capacitances, only the input base pad capacitance is added to the extracted base/emitter capacitance.

In emitter resistance extraction using the  $Z$ -parameter method, the base resistance adds a correction term to the extracted emitter resistance. The error should be fairly small for high-speed HBTs. The estimated external emitter resistance  $R_E$  will be larger than the actual value by a few percent. In emitter resistance extraction using the  $Y$ -parameter method, the extracted total emitter resistance is too high by a factor of  $1/\alpha$ . Base resistances further add to the apparent external emitter resistance. For most accurate emitter resistance extraction using either method, the base resistance and current gain must also be determined.

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